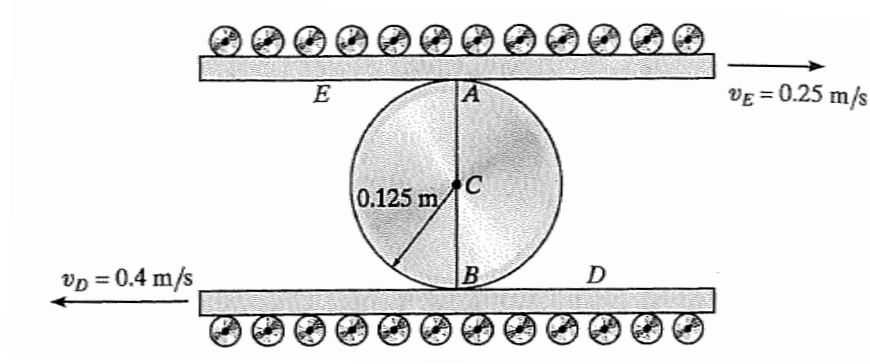


Dynamics Doctoral Qualifying Exam

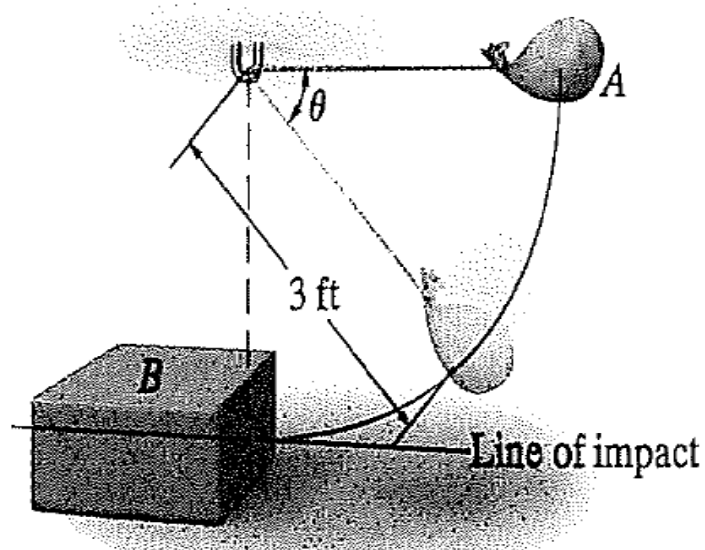
Time allowed: 2 hours

- Closed book and closed notes; one sheet (8.50 x 11.00 in, 2-sided) of formulas is allowed
- There are 4 problems worth a total of 100 points
- You MUST show and explain work to get credit
- Proceed in a linear fashion down the page – underlining your final answer
- Calculator allowed
- Laptops, cell phones, and similar electronic devices are not allowed
- Caution – usually the costliest mistake on a dynamics exam is not identifying the correct method (conservation of energy, $F=ma$, etc.) to solve the problem

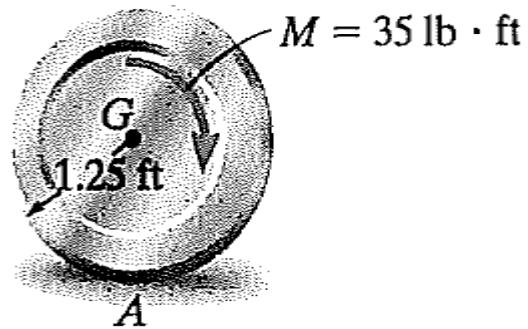
1. (25) The cylinder shown rolls without slipping between the two moving plates E and D . Determine the angular velocity, ω and the velocity of its center, v_c .



2. (25) The bag A weighing 6 lb is released from rest at the position $\theta = 0^\circ$ as shown in the figure. After falling to $\theta = 90^\circ$, it strikes an 18 lb box, B . If the coefficient of restitution between the bag and box is $e = 0.5$ determine the velocities of the bag and box just after impact.



3. (25) The 50 lb wheel shown has a radius of gyration, $k_G = 0.70\text{ ft}$. If a $35\text{ lb}\cdot\text{ft}$ couple is applied to the wheel, determine the acceleration of its mass center, a_G . The coefficients of static and dynamic friction between the wheel and the plane at A are $\mu_s = 0.3$ and $\mu_k = 0.25$ respectively.



4. (25) The 10 kg rod AB shown in the figure is constrained so that its ends move in the horizontal and vertical slots. The spring has a stiffness of $k=800\text{ N/m}$ and is unstretched when $\theta=0^\circ$. Determine the angular velocity of AB , ω , when $\theta=0^\circ$. if the rod is released from rest when $\theta=30^\circ$. Neglect the mass of the slider blocks. (For a uniform bar of length L and mass, m - $I_G=(1/12)mL^2$)

